

# Lecture: Information Frictions and Investment

**Advanced Macroeconomics**  
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# Theories of investment with financial frictions:

- An important friction is asymmetric information between borrowers and lenders
  - Hidden effort (**moral hazard**): Potential investors (managers) must have the right incentives
  - Private information (**adverse selection**): Potential investors know more about the project or the firm than financiers
- This asymmetric information has implications for investment

# Preview of the results:

- Key implication: **Limited pledgeability** and borrowing constraints:

**1. Net worth channel** in investment

**2. Financial (balance sheet) shocks** matter for macro outcomes

**3. General equilibrium effects** (on the interest rate)

**4. Financial accelerator**

The plan is to:

- Use Holmstrom and Tirole (1998) “Private and public supply of liquidity”, JPE, a moral hazard model to illustrate 1,2
- A variant of Bernanke and Gertler (1989) “Agency costs, net worth and business fluctuations” AER, to illustrate 4

# Holmstrom and Tirole's moral hazard model

- Two dates:  $t \in \{0,1\}$ , and a single consumption good (dollar)
- Two types of agents: financiers (F) and potential investors or entrepreneurs (E).
- Both types have linear preferences:  $U = C_1 + \beta C_2$
- F's have a large endowment. Competitive loan market ensures the interest rate is  $1/\beta$ . Later we endogenize this.
- Each E has endowment (net worth)  $N$  at date 0. Has access to a **fixed** scale project:
  - Investing 1 at date 0 yields output at date 1.
  - Assume  $1 > N$  so that the project needs financing

Fundamental problem: **mismatch of ideas and resources**

# Moral hazard: E can misbehave

- Suppose project either succeeds: yielding  $\frac{R}{p_H}$ , or fails: yielding 0.
- E may shirk and choose a different project (don't exert effort, another project, private benefits)
- Two versions of the project:

Project	Good	Bad
Private Benefit	0	$B > 0$
Prob. of success	$p_H$	$p_L < p_H$

- Information friction: **E's project choice is not observable to F's**

# A contract specifies the division of the output

- A contract specifies the partition of the output (in case of success) between F and E:

$$\frac{R^F}{P_H} \text{ and } \frac{R^E}{P_H}, \text{ with } R^F + R^E = R$$

- Assume

$$\beta \left( p_L \frac{R}{P_H} + B \right) < 1 < \beta R$$

- so the project is positive NPV if E behaves, but negative NPV otherwise

# Constraints

- **F's participation constraint (PC)**

$$\beta p_H \frac{R^F}{p_H} = 1 - N$$

F's receives the market return on her lending

- **E's incentive constraint (IC)**

$$p_H \frac{R^E}{p_H} \geq p_L \frac{R^E}{p_H} + B$$

- Which can be written as

$$R^E \geq \frac{p_H}{\Delta p} B$$

Next: For good management, E must have “**skin in the game**”

## Limited pledgeability

- Combining the last inequality with  $R^F + R^E = R$ , we obtain the **limited pledgeability (LP) constraint**:

$$R^F \leq \rho \equiv R - \frac{P_H}{\Delta p} B$$

where  $\rho$  is the (expected) **pledgeable output**

Limited pledgeability says that due to frictions not all returns can be promised to F

**Limited pledgeability is the key difference from the frictionless benchmark**



# Limited pledgeability generates a borrowing constraint

- Combining LP with PC, we obtain:

$$1 - N \leq \beta\rho$$

**Borrowing constraint:** E can only borrow up to the pdv of the pledgeable output

- Some positive NPV projects may not be undertaken
- Whether or not this happens depends on E's net worth

And generates a “net worth channel in investment”

- Rewrite the last inequality as:

$$N \geq \bar{N} = 1 - \beta\rho$$

**Net worth channel:**

- E's with sufficient net worth receive financing and invest
- E's with insufficient net worth,  $N < \bar{N}$ , are denied credit

## Credit rationing: markets clear with quantities

- E's with  $N < \bar{N}$  are willing to pay a higher interest rate (i.e. to promise a higher  $R^F$ )
- But F's do not accept this because of adverse incentives

**Credit rationing:** when prices have incentives (or information) effects, credit markets may clear with quantities rather than prices.

# Holmstrom and Tirole's model: flexible scale version

- Slight difference for investment technology: scale is flexible
- Investing  $I$  units in the project yields  $\frac{R}{p_H} I$  units in case of success and 0 units in case of failure

- Two versions of the project:

Project	Good	Bad
Private Benefit	0	$BI > 0$
Prob. of success	$p_H$	$p_L < p_H$

- Private benefit also scales up with investment (for simplicity)

## E chooses the investment level and a feasible contract

- E with net worth  $N$  invests  $I \geq N$ . Now choice variable.
- As before, IC leads to **limited pledgeability**:

$$R^F \leq \rho \equiv R - \frac{p_H}{\Delta p} B$$

- Combined with PC generates a **borrowing constraint (BC)**

$$I - N \leq \frac{\rho I}{1 + r}$$

- **E's problem:** Choose  $I \geq N$  that maximizes her payoff,  $RI - (1 + r)(I - N)$  subject to BC

# Investment depends on E's net worth

- Assume:  $\rho < 1 + r < R$
- RHS ensures that project is worth undertaking. LHS ensures the project is not self financing
- This implies E invests up to the maximum possible scale

$$I = \frac{N}{1 - \rho / (1 + r)}$$

This is just a restatement of the net worth channel with flexible scale

- This aggregates over all E's:  $I^{agg} = \frac{N^{agg}}{1 - \rho / (1 + r)}$

Aggregate investment depends on the net worth of E's in the economy

# Implications of the net worth channel

- **Financial (balance sheet) shocks** that lower E's net worth will lower investment:
  - A transfer of net worth from E's to F's (e.g. nominal contracts and Fisher's debt deflation)
  - Shocks to E's assets (e.g. subprime shock). Amplified by leverage
- Balance sheet effects will also amplify other shocks
  - Deterioration of E's net worth because of low profits in a recession
  - These 2 effects would not be present in a representative agent framework
- Next: General equilibrium implications (endogeneize the interest rate)

## Equilibrium in the asset market: Supply side

- To endogeneize  $r$ , think of the equilibrium in the asset market
- Recall that the interest rate is the inverse of the asset prices
- We have the **supply of assets** in terms of pledgeable output)

$$S^{asset}(r) = \rho I^{agg} = \frac{\rho N^{agg}}{1 - \rho / (1 + r)}$$

The E's offer more assets the lower is  $r$



## Equilibrium in the asset market: Demand side

- For the demand side suppose F's preferences are:  $u(C_0^F) + \beta u(C_1^F)$
- Consider the optimal savings decision:

$$\begin{aligned} \max_{C_0^F, C_1^F} \quad & u(C_0^F) + \beta u(C_1^F) \\ \text{s.t.} \quad & C_0^F + \frac{C_1^F}{1+r} \leq N^F \end{aligned}$$

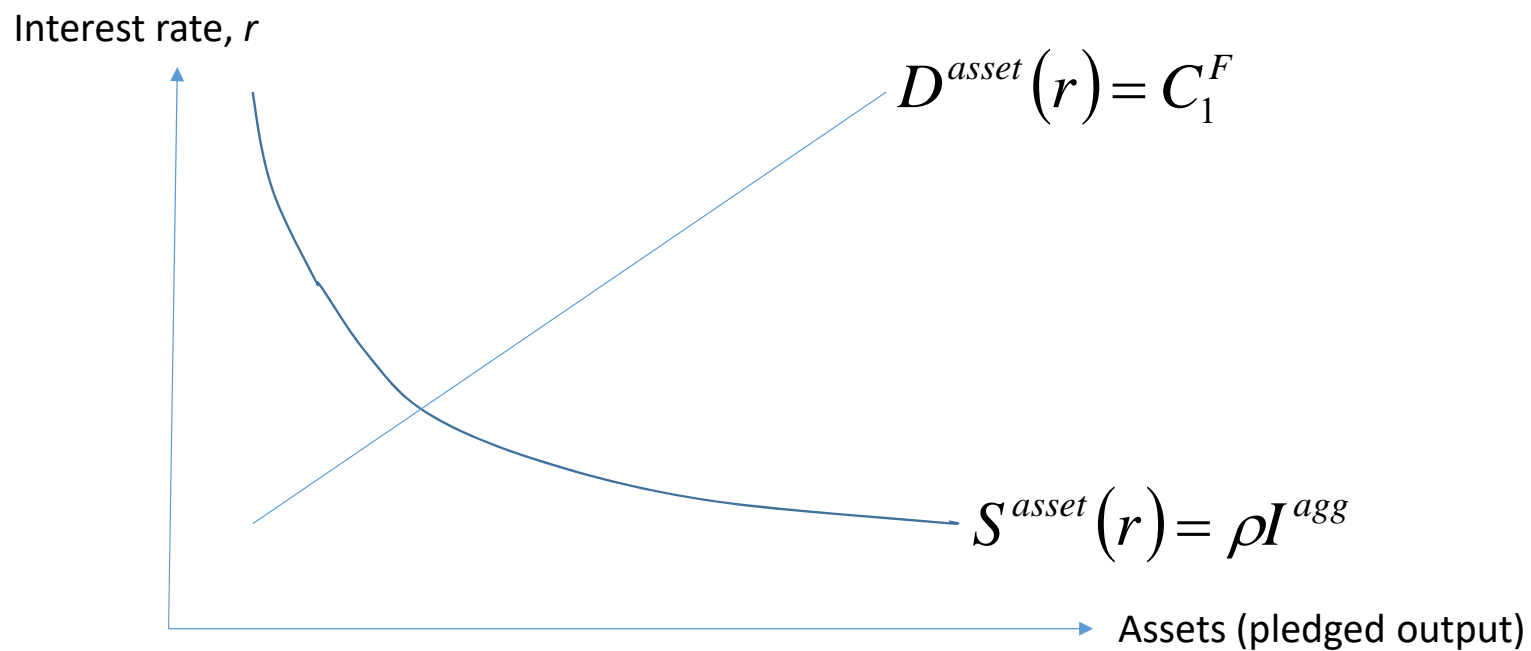
The solution is characterized by the Euler equation:

$$u'(C_0^F) = (1+r)\beta u'(C_1^F)$$

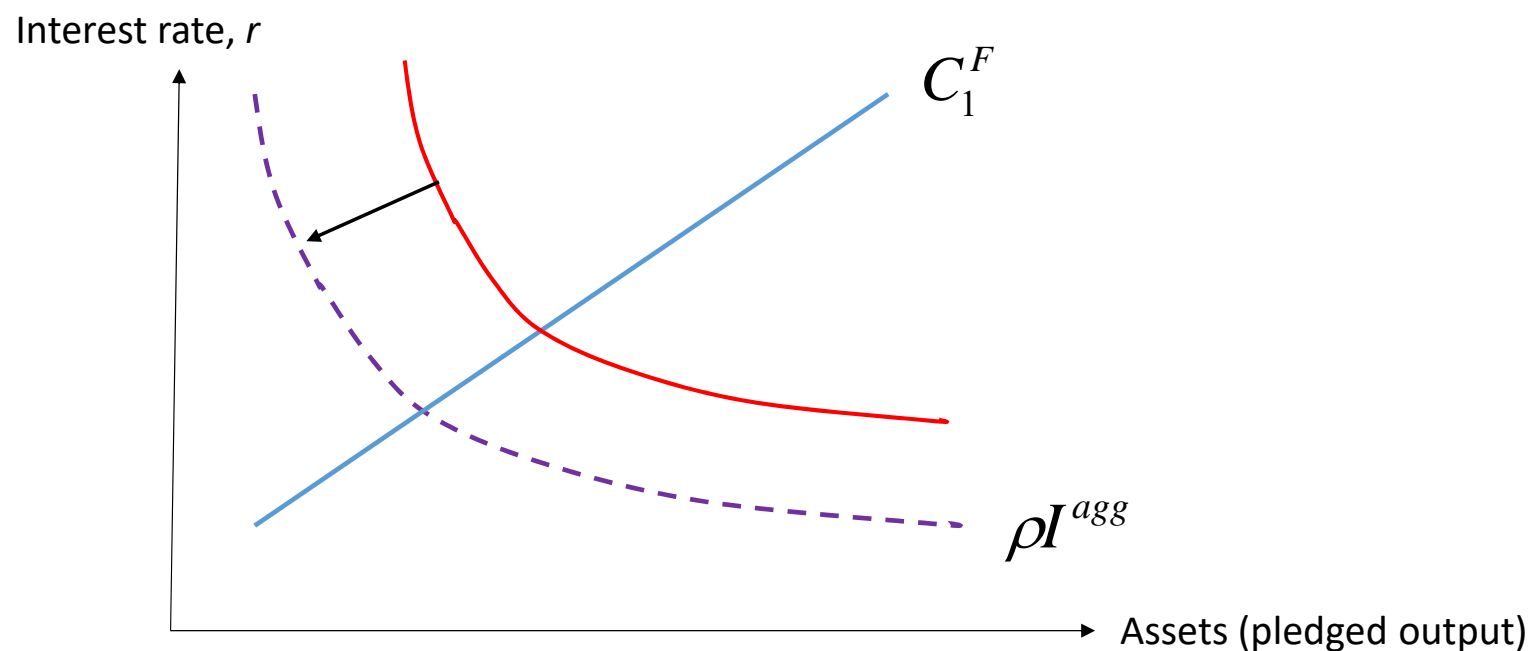
The demand for assets is given by:  $D^{asset}(r) = C_1^F$

It is increasing in  $r$

# Equilibrium in the asset market

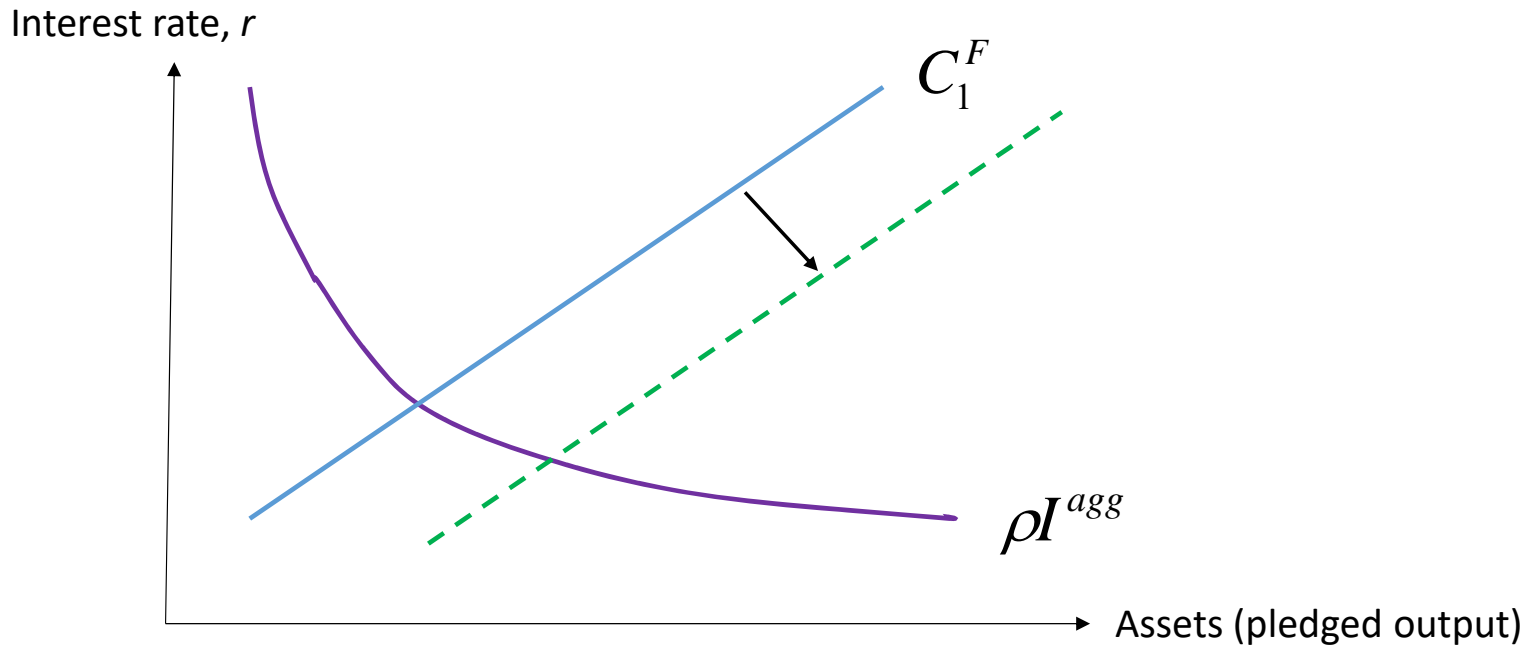


# Reduction in E's net worth lowers investment, assets supply, and interest rate



A reduction in  $\rho$  has the same effect

Reduction in savings demand (i.e. precautionary motive) increases credit and lowers interest rate



# Balance sheet channel has dynamic implications

- Bernanke and Gertler (1989) put financial frictions into a dynamic equilibrium macro model and emphasize the role of the balance sheet channel in the origination and the **propagation** of shocks
- **Persistence and propagation of shocks**
  - E's net worth likely to be procyclical (less solvent during bad times)
  - A recession will erode net worth, which in turn will reduce investment and propagate the recession (and vice versa for boom)
- Next: Holmstrom and Tirole model in a dynamic macro environment to illustrate the propagation mechanism

# Consider a standard OLG model

- Consider an OLG economy with a single consumption good (euros) and two factors: capital and labor
- Generation  $t$  agents live 2 periods: Continuum of 1 (total)
- E's and F's with preferences:  $C_{t,1} + \frac{1}{1+r} C_{t,2}$ , (back to exogenous  $r$ )
- Production technology (consumption):  $A_t F(K_t, L_t)$ 
  - Suppose (for simplicity) that  $A_t$  is i.i.d. with mean  $\bar{A}$
  - Suppose (for simplicity) that capital depreciates completely after 1 period
- Labor is supplied inelastic by the young,  $L_t = 1$
- Factor markets are competitive:

$$R_t = A_t F_K(K_t, 1) \text{ and } w_t = A_t F_L(K_t, 1)$$

# Benchmark: equilibrium without frictions

- Start with a benchmark with no frictions
- Young E's have access to an investment technology:  $I_t$  (consumption good) invested at date  $t$  generate  $I_t / p_H$  units of capital date  $t+1$  with probability  $p_H$  (0 otherwise)
- Continuum with no aggregate uncertainty implies:

$$K_{t+1} = I_t (\# \text{Entrepreneurs})$$

- Equilibrium capital found from:

$$1 + r = E[R_{t+1}] = \bar{A} F_K(K^*, 1)$$

- Note that  $K_{t+1} = K^*$  is independent of  $A_t$
- **Without frictions, temporary productivity shocks have no effect on investment**

# Introduce asymmetric information

- Assume E's have mass  $\eta$ , and F's have mass  $1 - \eta$
- E's and F's net worth is their labor income

$$N_t = N_t^E = \eta w_t \quad \text{and} \quad N_t^F = (1 - \eta) w_t$$

**E's net worth is endogenous**



# E's investment is subject to moral hazard

- Next suppose E's are subject to moral hazard as in Holmstrom and Tirole:

Project	Good	Bad
Private Benefit	0	$BI > 0$
Prob. of success	$p_H$	$p_L < p_H$

- Still no aggregate uncertainty (in a symmetric equilibrium)

$$K_{t+1} = I_t(1-\eta)$$

# E's contract is isomorphic to previous model

- Expected return from success:

$$E_t(R_{t+1}) \frac{I_t}{P_H} = \bar{A} F_K(K_{t+1}, 1) \frac{I_t}{P_H}$$

which is deterministic

- E's private benefit:  $BI_t$
- Given  $N_t$ , E chooses the contract:  $(I_t \geq N_t, R_{t+1}^{E, \text{expected}}, R_{t+1}^{F, \text{expected}})$
- To maximize her payoff subject to:
  - Resource constraint  $R_{t+1}^{E, \text{expected}} + R_{t+1}^{F, \text{expected}} = E[R_{t+1}]$  (with linear prefs, exact distribution of returns not important)
  - E's (IC):  $R_{t+1}^{E, \text{expected}} \geq p_H B / \Delta p$
  - F's (PC):  $R_{t+1}^{F, \text{expected}} I_t = (I_t - N_t)(1+r)$
- E's problem is the same as in the two period version (with  $ER_{t+1}$  replacing  $R$ )

# Definition of equilibrium

- Given the initial stock of capital  $K_0$  an equilibrium is a vector of factor allocations  $\{K_t, L_t = 1\}_{t=0}^{\infty}$ , prices  $\{R_t, w_t\}_{t=0}^{\infty}$  and contracts  $(I_t, R_{t+1}^{E, \text{expected}}, R_{t+1}^{F, \text{expected}})_{t=0}^{\infty}$  such that:
  - Factor markets clear
  - E's in each period make their investment and contract decisions optimally
  - Capital evolves as  $K_{t+1} = I_t(1 - \eta)$

Make parametric assumption such that

$$\rho_t \equiv E_t(R_{t+1}) - \frac{p_H B}{\Delta p} < 1 + r < E_t(R_{t+1})$$

# Investment is the solution to a fixed point theorem

- From the earlier analysis, we have

$$K_{t+1} = \frac{(1-\eta)N_t}{1-\rho_t/(1+r)}$$

Plugging in the definition of  $\rho_t$  and using  $E_t[R_{t+1}] = \bar{A}F_K(K_{t+1},1)$

$$K_{t+1} = \frac{(1-\eta)N_t}{1 - \left( \bar{A}F_K(K_{t+1},1) - \frac{p_H B}{\Delta p} \right) / (1+r)}$$

Under regularity conditions, there is a unique  $K^{next}(\cdot)$  s.t.  $K_{t+1} = K^{next}(N_t)$

The function  $K^{next}(N_t)$  is increasing in  $N_t$

Check these claims for the Cobb Douglas case:  $F(K_t,1) = K^\alpha$

# Financial accelerator and the propagation of shocks

- Plugging in  $N_t = \eta A_t F_L(K_t, 1)$  we obtain:

$$K_{t+1} = K^{next}(\eta A_t F_L(K_t, 1))$$

- **Persistency and propagation of shocks:** next period capital stock (and investment) is increasing in  $A_t$  and  $K_t$ . Temporary shocks have long lasting effects, in contrast with the frictionless benchmark:

$$A_t \downarrow \Rightarrow K_{t+1} \downarrow \Rightarrow K_{t+2} \downarrow \dots$$

- **Intuition (balance sheet channel):** shocks propagate through E's net worth:

$$A_t \downarrow \Rightarrow N_t \downarrow \Rightarrow K_{t+1} \downarrow \Rightarrow N_{t+1} \downarrow \Rightarrow K_{t+2} \downarrow \dots$$

This is known as the **financial accelerator**. The particular propagation illustration in B-G (through wages) is not convincing. But the mechanism is more general.

# Taking stock: Net worth channel and investment

- Asymmetric information between financiers and potential investors.
- Key implication is borrowing constraints and limited pledgeability.  
Generate:
  - **Net worth channel** in investment
  - **Financial (balance sheet) shocks**
  - **GE effects:** Tightening of constraint reduces supply of assets, increases assets prices, and lowers the interest rate
  - **Financial accelerator** and the propagation of shocks